A STATISTICAL COMPARISON BETWEEN NON-PARAMETRIC AND PARAMETRIC STABILITY MEASURES

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ABSTRACT

The computation of type I error (α) and power of the test useful in evaluating the merits of various stability measures are discussed. Performances of non-parametric measures vis-a-vis parametric measures have been assessed based on these criteria. **Key words :** Stability, parametric measures, non-parametric measures

Non-parametric measures are widely employed in the selection of crop varieties especially when the interest lies in genotypes, which excel in both yield and stability. However, it is a known fact that the non-parametric methods are less powerful than their parametric counterparts. Nevertheless, very little work has been done in the direction of comparing the performance of non-parametric measures *vis a vis* parametric measures. A comparative study will be quite useful because, if it is found that the loss in efficiency of the non-parametric approach is marginal in the situations, which are commonly encountered, these measures can be safely recommended.

Thennarasu[1] had proposed four non-parametric measures and shown that two of them performed better than other measures. He, however, did not consider their performance relative to the common parametric measures. In this paper we concentrate on the relative merits of non-parametric and parametric measures under different practical situations, the merits being judged on the basis of two criteria namely, (i) convergence of observed \propto (Type-I error) to the postulated \propto and (ii) the power of the test.

MATERIALS AND METHODS

Consider t genotypes having performance tested in s environments. In non-parametric analysis of GE interaction we deal with ranks of genotypes separately for each of these s environments. The rank of a genotype in a particular environment

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cannot be based purely on the phenotypic values (Y_{ij}) because the stability has to be measured independently of the genotypic effect. Therefore, r_{ij} the rank of the *i*th genotype in the *j*th environment is determined on basis of the corrected phenotypic values y_{ij} , namely $(Y_{ij} - \overline{Y}_i)$, \overline{Y}_i . being the mean performance of the *i*th genotype. The ranks obtained from these corrected Y_{ij} 's depend only on the GE interaction and error components and these are tabulated in Table 1.

Genotype		Environment												
	e ₁	e ₂	e ₃		e _j		e _s	Mean						
<i>8</i> ₁	<i>r</i> ₁₁	r ₁₂			r_{1j}		r_{1s}	\overline{r}_{1}						
82	<i>r</i> ₂₁	r ₂₂			<i>r</i> _{2j}		r _{2s}	$\overline{r}_{2.}$						
						•••	•							
<i>8i</i> ·	r_{i1}	r _{i2}	•		r_{ij}		r _{is}	$\overline{r}_{i.}$						
	•													
<i>8</i> _{<i>t</i>}	r_{t1}	r_{t2}		•••	r_{tj}	•••	r _{ts}	$\overline{r}_{t.}$						
Mean	$\frac{t+1}{2}$	$\frac{t+1}{2}$			$\frac{t+1}{2}$		$\frac{t+1}{2}$	$\overline{r} = \frac{t+1}{2}$						

Table 1. Ranks of t genotypes in s environments

Using the rank values and rank means defined in Table 1, Thennarasu[1] purposed the following stability measures:

$$NP_{i}(1) = \frac{1}{S} \sum_{j=1}^{S} |r_{ij} - M_{di}| \qquad ... (1)$$

$$NP_{i}(2) = \frac{1}{S} \left[\sum_{j=1}^{s} |r_{ij} - M_{di}| / M_{di}^{*} \right] \qquad \dots (2)$$

$$NP_{i}(3) = \frac{\sqrt{\Sigma (r_{ij} - \bar{r}_{i})^{2} / S}}{\bar{r}_{i}^{*}} \qquad ... (3)$$

$$NP_{i}(4) = \frac{2}{S(S-1)} \left[\sum_{j=1,j'=j+1}^{S-1} |r_{ij} - r_{ij'}| / \overline{r}_{i.} \right] \qquad \dots (4)$$

In this investigation, these non-parametric measures are compared, for their performance, with Huhn[2] measure,

$$NP_{i}(5) = \frac{1}{S-1} \sum_{j} (r_{ij} - \bar{r}_{i})^{2} \qquad \dots (5)$$

as well as the parametric measures b_i , S_{di}^2 , W_i , r_i^2 and σ_i^2 . In the formulae, the quantities \overline{r}_i and M_{di} are the mean and median ranks respectively of the *i*th genotype, obtained from the corrected Y_{ij} s while \overline{r}_i^* and M_{di}^* are the same parameters computed from the uncorrected Y_{ij} s. For ranking purpose, the smallest y_{ij} in a particular environment is given rank one, the next higher value, rank two, and so on. Here, $NP_i(1)$ denotes magnitude of measure NP(1) for the *i*th genotype, and similarly for the other measures. In the course of further discussion the parametric measures will be denoted by P(1), P(2), P(3), P(4) and P(5) respectively. We shall now consider the simulation procedure involved in the computation of type I error and power of the test.

Determination of type I error and power of the test

To apply the test of significance of any measure through χ^2 test or by normal *Z* test, it is necessary that the stability measure should follow normal distribution. For ensuring non-erroneous selection of genotypes, the power of the test should be high. In order to find out a better stability parameter for a particular situation, comparison is carried out, making use of these distributional properties. To examine whether the normality holds or not a simulation programme is run and the observed and expected probability of type I error (∞) for various stability measures, parametric as well as non-parametric, are compared. The soundness of the normal approximation for each of these measures is thereby assessed. A comparison is also made in terms of their power of the test. The essential details of the simulation procedure are given in the following paragraphs.

Simulation of variate values

According to Nassar *et al.*, [3] the ultimate distributional properties and the power of *F* test do not change much when the variate values are generated on computer and this is the motivation for the adoption of the procedure for the present investigation. The simulation of normal variate with general mean μ and error standard deviation σ_e is carried out in two stages. In the first stage, the standard uniform variates are generated which is further used to generate standard normal variates. The generation of standard uniform variate starts with the use of a random seed value, which allows the first function to generate a random number. The seed value used in the generation of first random number will change itself and produces

an entirely different random number, and this process continues. The generated random number in this function, every time, gets converted into a standard uniform variate, which will be used in second stage.

The second stage is the generation of normal variates with specified µ and σ_{e} values and this is achieved as follows. A second subroutine receives generated standard uniform variates from the first stage and converts them into a standard normal variates. These standard normal variates are used in the main programme to generate normal variables with a given mean and standard deviation. For generating a normal variate under the null hypothesis that all genotypes are equal in their effects, with mean μ and error variance σ_{ν} , the model needs to include only the environmental and error effects. Therefore, in the generation of a single normal value (Y_{ij}) , the programme invokes both the subroutines twice. But the generation of the variate values under the alternative hypothesis that the genotypes are not stable over the environments involves the inclusion of the effects of genotype, environment and GE interaction in the model. Thus the programme requires the invoking the subroutine four times one each for genotypic, environmental, interaction and error effects. The programme, therefore, takes more running time under alternative hypothesis than under null hypothesis. Adopting this procedure the probability of type I error and power of the test are studied in the following paragraphs.

Determination of type I error

The fact that the stability measures developed based on ranks can be approximated to normal distribution at least in the tail ends of the distribution [4] has helped in the development of the significance test for equality of stability values. The simulation procedure for the determination of Y_{ij} values under null hypothesis is considered in what follows:

Under the null hypothesis the performance of *i*th genotype in *j*th environment can be expressed as

$$Y_{ij} = \mu + e_j + \varepsilon_{ij} \qquad \dots (6)$$

where, μ is the over all population mean,

 e_i is the effect of environment j (j= 1, 2, ..., s)

 ε_{ij} is the random error associated with *i*th genotype (*i* = 1, 2, ..., *t*) and *j*th environment and distributed with mean zero and variance σ_{e}^{2}

Since the environmental effect is same for all the genotypes, e_j has no influence on the null hypothesis in so far as the non-parametric measures are concerned and so in the generation of Y_{ij} values e_j can be conveniently assumed to be zero. For the simulation of the requisite data, the parametric values of μ and σ_e^2 were taken from the extensive data from All India Coordinated Project on Pearl millet. Assuming the grain yields to be normally distributed, the required normal variates (Y_{ij}) were generated as per the procedure, given above taking $\mu = 1984$ and $\sigma_e^2 = 152.22$ and $\sigma_F^2 = 1121$.

The simulation programme is run for generating sets of $t \times s$ observations, coming from t genotypes (8, 10, ..., 24) and s environments (5, 10, 15). For each (t, s) combination the data are generated using three different random seeds thereby obtaining 3 sets of ts observations to serve as 3 replications. For each replication of a specified ts observations, the values of non-parametric stability measures NP(1) to NP(5) and also of the parametric measures considered are arrived at. This yields different sets of $3 \times t$ values, one for each stability parameter, and each set is subjected to a one way ANOVA for testing the genotypic differences if any. For each (t, s) combination the entire procedures is repeated for 1000 (in a few cases, 5000 times) times and the number of times the observed F ratios exceed the table F value is determined. This number expressed as a proportion is our observed type I error. The observed \propto is computed for different expected levels of significance ($\propto = 0.01, 0.05$). For these expected \propto levels the table values of F with degrees of freedom (t - 1) and 2t are taken as critical values. For the comparison of observed \propto with a specified expected \propto has been presented in Tables 2 to 13. These are tabulated for the different stability measures mentioned above for different combination of t and s.

Power of the test

For the comparison of the stability measures NP(1) to NP(5) with the parametric measures mentioned in the previous section in terms of their power efficiency a simulation programme was run under the full model

$$Y_{ij} = \mu + g_i + e_j + (ge)_{ij} + \varepsilon_{ij}$$

where the symbols have their usual meanings. The generation of variate values is carried out as explained earlier. For the simulation purpose the parametric values as determined from the real data on pearl millet have been made use of. Data are generated for different combination of t (8, 12, 16, 20 and 24) and s (5, 10 and 15). With the help of the $t \times s$ simulated normal values t genotypic stability values are

Table 2.	Comparison between observed and expected Type I error (∞) for different
	number of genotypes (t) tested in $s = 5$ environments for various
	non-parametric measures

		Expected	$d \propto = 0.01$		
t	NP(1)	NP(2)	NP(3)	NP(4)	NP(5)
8	0.0167*	0.0170	0.0240	0.0231	0.0223
10	0.0171	0.0143	0.0217	0.0219	0.0167
12	0.0141	0.0137	0.0194	0.0193	0.0163
14	0.0140	0.0133	0.0181	0.0181	0.0150
16	0.0123	0.0130	0.0165	0.0162	0.0141
18	0.0117	0.0120	0.0141	0.0171	0.0141
20	0.0114	0.0121	0.0137	0.0132	0.0140
22	0.0122	0.0120	0.0129	0.0121	0.0123
24	0.0113	0.0099	0.0131	0.0115	0.0121

*An observed value represents Pr $[F > F_{.01, (t-1), 2t}]$

Table 3.	Comparis	son between o	bserve	ed and o	expecte	d Ty _F	pe I error (∝) :	for o	lifferent
	number o	of genotypes	(t) te	ested in	n <i>s</i> =	10 e	nvironments	for	various
	non-parar	metric measur	es						

		Expe	ected $\propto = 0.01$			
t	NP(1)	NP(2)	NP(3)	NP(4)	NP(5) .	
8	0.0240	0.019	0.027	0.031	0.023	
10	0.0230	0.017	0.026	0.029	0.021	
12	0.0200	0.013	0.023	0.028	0.021	
14	0.0190	0.012	0.021	0.024	0.020	
16	0.0170	0.011	0.019	0.019	0.021	
18	0.0150	0.009	0.018	0.018	0.019	
20	0.0120	0.011	0.018	0.015	0.017	
22	0.0110	0.012	0.014	0.014	0.016	
24	0.0130	0.013	0.015	0.016	0.015	

Table 4.	Compari	son	between o	bser	ved and	d ex	cpe	ecte	ed T	'ype I error (∝)	for	different
	number	of	genotypes	(<i>t</i>)	tested	in	\$	=	15	environments	for	various
	non-para	ime	tric measur	es								

		Expected	∝ = 0.01		
t	NP(1)	NP(2)	NP(3)	NP(4)	NP(5)
8	0.0230	0.0190	0.027	0.0330	0.0270
10	0.0200	0.0200	0.028	0.0300	0.0260
12	0.0160	0.0180	0.029	0.0280	0.0220
14	0.0150	0.0170	0.022	0.0250	0.0230
16	0.0140	0.0160	0.019	0.0240	0.0170
18	0.0120	0.0160	0.018	0.0220	0.0160
20	0.0120	0.0150	0.014	0.0180	0.0150
22	0.0110	0.0130	0.012	0.0180	0.0150
24	0.0130	0.0110	0.017	0.0220	0.0150

*An observed value represents Pr $[F > F_{.01, (t-1), 2t}]$

Table 5. Comparison between observed and expected Type I error (\propto) for different number of genotypes (t) tested in s = 5 environments for various non-parametric measures

		Expe	cted $\propto = 0.05$			
t	NP(1)	NP(2)	NP(3)	NP(4)	NP(5)	
8	0.0650	0.0690	0.0890	0.0810	0.6730	
10	0.0613	0.0590	0.0880	0.0840	0.0700	
12	0.0631	0.0570	0.0740	0.0790	0.0720	
14	0.0610	0.0587	0.0780	0.0720	0.0660	
16	0.0590	0.0530	0.0710	0.0780	0.0650	
18	0.0560	0.0460	0.0690	0.0720	0.0570	
20	0.0570	0.0510	0.0670	0.0640	0.0590	
22	0.0540	0.0540	0.0640	0.0670	0.0610	
24	0.0530	0.0520	0.5900	0.0610	0.0610	

Table 6.	Compari	ison	between o	bsei	rved and	d ex	pect	ed T	'ype I error (∝)	for (different
	number	of	genotypes	(<i>t</i>)	tested	in	<i>s</i> =	10	environments	for	various
	non-para	ame	tric measur	es							

		Expe	ected $\propto = 0.05$			
t	NP(1)	NP(2)	NP(3)	NP(4)	NP(5)	
8	0.083	0.077	0.102	0.087	0.098	
10	0.076	0.074	0.092	0.081	0.082	
12	0.065	0.071	0.079	0.082	0.074	
14	0.063	0.080	0.081	0.073	0.069	
16	0.059	0.060	0.064	0.067	0.068	
18	0.057	0.061	0.068	0.064	0.056	
20	0.053	0.058	0.059	0.062	0.057	
22	0.060	0.057	.0.060	0.061	0.053	
24	0.052	0.057	0.063	0.060	0.063	

*An observed values represents Pr $(F > F_{.05, t-1, 2t})$

Table 7.	Compari	son	between o	bsei	rved an	d e	cpe	ecte	ed T	'ype I error (∝)	for	different
	number	of	genotypes	(<i>t</i>)	tested	in	S	=	15	environments	for	various
	non-para	ıme	tric measur	es								

		Expe	ected $\propto = 0.05$			
t	NP(1)	NP(2)	NP(3)	NP(4)	NP(5)	
8	0.0920	0.066	0.089	0.1160	0.093	
10	0.0810	0.065	0.082	0.092	0.094	
12	0.0840	0.061	0.081	0.086	0.092	
14	0.0820	0.062	0.075	0.072	0.089	
16	0.0790	0.059	0.071	0.074	0.081	
18	0.0770	0.057	0.062	0.069	0.076	
20	0.0650	0.057	0.061	0.064	0.075	
22	0.0620	0.052	0.058	0.063	0.068	
24	0.0590	0.053	0.058	0.063	0.064	

	Expected $\propto = 0.01$									
t	P(1) P(2) P(3) P(4) P(5)									
8	0.0164	0.0153	0.0186	0.0247	0.0274					
10	0.0159	0.0146	0.0181	0.0221	0.0247					
12	0.0143	0.0143	0.0174	0.0193	0.0276					
14	0.0131	0.0137	0.0168	0.0182	0.0202					
16	0.0127	0.0133	0.0163	0.0169	0.0163					
18	0.0124	0.0121	0.0149	0.0154	0.0158					
20	0.111	0.0120	0.0144	0.0147	0.0150					
22	0.0112	0.0122	0.0139	0.0142	0.0167					
24	0.0091	0.0126	0.0141	0.0137	0.0146					
26	0.0117	0.0127	0.0132	0.0122	0.0131					

Table 8. Comparison between observed and expected Type I error (∞) for different number of genotypes (t) tested in s = 5 environments for various parametric measures

*An observed values represents Pr $(F > F_{.01, t-1, 2t})$

Table 9. Comparison between observed and expected Type I error (\propto) for different number of genotypes (t) tested in s = 10 environments for various parametric measures

	Expected $\propto = 0.01$								
t	P(1)	P(2)	P(3)	P(4)	P(5)				
8	0.0143	0.0156	0.0147	0.0167	0.0233				
10	0.0143	0.0155	0.0147	0.0142	0.0211				
12	0.0139	0.0147	0.0131	0.0131	0.0192				
14	0.0137	0.0140	0.0137	0.0124	0.0171				
16	0.0134	0.0134	0.0129	0.0113	0.0167				
18	0.0121	0.0130	0.0133	0.0083	0.0151				
20	0.0124	0.0127	0.0120	0.0081	0.0130				
22	0.0119	0.0126	0.0124	0.0117	0.0124				
24	0.0107	0.0121	0.0127	0.0116	0.0101				

	Expected $\propto = 0.01$									
t	P(1)	P(2)	P(3)	P(4)	P(5)					
8	0.0152	0.0158	0.0201	0.0143	0.0221					
10	0.0147	0.0156	0.0197	0.0142	0.0206					
12	0.0147	0.0144	0.0194	0.0142	0.0174					
14	0.0131	0.0143	0.0186	0.0134	0.0163					
16	0.0134	0.0140	0.0177	0.0127	0.0170					
18	0.0119	0.0139	0.0163	0.0119	0.0161					
20	0.0107	0.0132	0.0160	0.0110	0.0156					
22	0.0113	0.0130	0.0154	0.0126	0.0147					
24	0.0117	0.0134	0.0154	0.0120	0.0144					

Table 10. Comparison between observed and expected Type I error (\propto) for different number of genotypes (t) tested in s = 15 environments for various parametric measures

*An observed values represents Pr $(F > F_{.01, t-1, 2t})$

Table	11.	Compari	son	between ol	bser	ved and	l ex	pe	cteo	d T	ype I error (∝)	for o	lifferent
		number	of	genotypes	(<i>t</i>)	tested	in	S	=	5	environments	for	various
		paramet	ric 1	neasures									

t	P(1)	P(2)	P(3)	P(4)	P(5)				
8	0.0640	0.0611	0.0771	0.0744	0.0834				
10	0.0621	0.0607	0.0723	0.0671	0.0810				
12	0.0603	0.0600	0.0694	0.0663	0.0807				
14	0.0574	0.0591	0.0641	0.0644	0.0741				
16	0.0543	0.0570	0.0617	0.0610	0.0674				
18	0.0531	0.0574	0.0609	0.0576	0.0631				
20	0.0540	0.0539	0.0603	0.0549	0.0647				
22	0.0529	0.0530	0.0584	0.0537	0.0614				
24	0.0613	0.0517	0.0592	0.0532	0.0600				

Expected $\propto = 0.05$

Table	12.	Compari	son	between o	bser	ved and	d ex	cpe	ecte	ed T	ype I error (∝)	for a	lifferent
		number	of	genotypes	(<i>t</i>)	tested	in	\$	=	10	environments	for	various
		parameti	ric 1	measures									

t	P(1)	P(2)	P(3)	P(4)	P(5)	
8	0.0634	0.0621	0.0723	0.0717	0.0804	
10	0.0630	0.0601	0.0701	0.0642	0.0775	
12	0.0567	0.0607	0.0664	0.0636	0.0713	
14	0.0561	0.0602	0.0621	0.0619	0.0642	
16	0.0547	0.0567	0.0617	0.0581	0.0531	
18	0.0540	0.0566	0.0601	0.0580	0.0632	
20	0.0531	0.0544	0.0602	0.0553	0.0606	
22	0.0531	0.0540	0.0601	0.0551	0.0582	
24	0.0546	0.0540	0.0600	0.0550	0.0580	

Expected $\propto = 0.05$

*An observed values represents Pr $(F > F_{.05, t-1, 2t})$

Table 13. Comparison between observed and expected Type I error (∞) for different number of genotypes (t) tested in s = 15 environments for various parametric measures

	Expected $\propto = 0.05$									
t	P(1)	P(2)	P(3)	P(4)	P(5)					
8	0.0679	0.0622	0.0743	0.0736	0.0792					
10	0.0664	0.0607	0.0712	0.0697	0.0687					
12	0.0643	0.0606	0.0683	0.0692	0.0632					
14	0.0611	0.0594	0.0642	0.0647	0.0631					
16	0.0613	0.0590	0.0621	0.0627	0.0624					
18	0.0600	0.0610	0.0624	0.0596	0.0622					
20	0.0604	0.0616	0.0617	0.0582	0.0613					
22	0.0597	0.0600	0.0623	0.0567	0.0607					
24	0.0603	0.0600	0.0614	0.0569	0.0600					

calculated for all the stability measures. In fact, we consider two additional set of $t \times s$ observations obtained from different seeds. These sets along with the first set serve as 3 replications of t genotypic stability values, which are analyzed by one way ANOVA for equal genotypic effects. The observed F value computed from the simulation is compared with the table F value with (t - 1), 2t degrees of freedom. This procedure is repeated for 1000 times (5000, in a few cases) and the number of times the observed F statistic from ANOVA exceed the tabular F values at each level of significance, \propto (0.01, 0.05) is worked out. The power of the test is determined there from. The values for different combinations of \propto , t and s are presented in Tables 14 to 17.

Table 14. Comparison of power of the test (in a one way ANOVA) for different combinations of number of genotypes (t) and number of environments (s) at $\infty = 0.01$ for non- parametric measures

· (e	G	E	$ G \times E$			
t	s	NP(1)	NP(2)	NP(3)	NP(4)	NP(5)	
8	5	0.411	0.373	0.337	0.495	0.379	
12	5	0.596	0.667	0.621	0.771	0.672	
16	5	0.751	0.764	0.772	0.932	0.819	
20	5	0.922	0.913	0.941	0.976	0.923	
24	5	0.982	0.952	0.987	1.000	0.964	
8	10	0.437	0.481	0.529	0.571	0.447	
12	10	0.622	0.733	0.812	0.842	0.779	
16	10	0.791	0.891	0.947	0.973	0.891	
20	10	0.849	0.974	1.000	1.000	0.967	
24	10	0.973	1.000	1.000	1.000	0.993	
8	15	0.399	0.533	0.462	0.610	0.311	
12	15	0.621	0.741	0.791	0.774	0.547	
16	15	0.724	0.839	0.877	0.831	0.721	
20	15	0.891	0.916	0.974	0.924	0.836	
24	15	0.967	0.953	0.981	0.988	0.951	

 μ (Mean) = 1984 σ_e^2 = 152.22 σ_G^2 = 97.08 σ_E^2 = 1121 $\sigma_{G \times E}^2$ = 324.44

RESULTS AND DISCUSSION

As the non-parametric measures are distribution free, these measures can be computed even when the genotype-environment data do not follow normal distribution. These are also resorted to when the nonlinear component of GE interaction is so large that the parametric measures fail to provide any meaningful interpretation of the stability factor. It is against this background, a comparison between non-parametric and parametric measures have been made through the simulation procedure outlined in the previous section. The observed values of type-I error (\propto) for the non-parametric measures, for different levels of expected \propto , genotype (t) and environment (s) numbers are presents in Tables 2 to 7. Similar values for the parametric case are given in Tables 8 to 13. From these tables it is evident that the agreement between observed and expected \propto is more striking in the case of non-parametric measures. As regards the convergence of observed to expected \propto it is faster in the case of NP(2) than the

Table 15. Comparison of power of the test (in a one way ANOVA) for different combinations of number of genotypes (t) and number of environment (s) at $\propto = 0.05$ for non- parametric measures.

μ (Mear	σ_e^2 = 1984 σ_e^2	$= 152.22 \sigma_G^2 =$	97.08 $\sigma_E^2 = 1$	$121 \ \sigma_{G \times E}^2 = 32$	4.44	
t	s	NP(1)	NP(2)	NP(3)	NP(4)	NP(5)
8	5	0.531	0.613	0.597	0.671	0.556
12	5	0.771	0.741	0.839	0.883	0.839
16	5	0.783	0.831	0.984	0.944	0.971
20	5	0.881	0.961	0.981	0.979	0.986
24	5	0.942	0.982	0.987	0.999	0.991
8	10	0.562	0.601	0.655	0.757	0.677
12	10	0.692	0.799	0.891	0.917	0.834
16	10	0.872	0.917	0.937	1.000	0.951
20	10	0.937	1.000	0.981	1.000	0.973
24	10	0.974	1.000	1.000	1.000	0.982
8	15	0.566	0.572	0.743	0.641	0.531
12	15	0.673	0.811	0.873	0.939	0.666
16	15	0.754	0.970	0.962	0.968	0.837
20	15	0.873	0.967	0.981	0.996	0.941
24	15	0.913	0.960	0.974	1.000	0.954

$$\mu$$
 (Mean) = 1984 σ^2 = 152.22 σ^2_{c} = 97.08 σ^2_{r} = 1121 σ^2_{c} = 324.44

remaining measures; for a small number of environments (s) it needs lesser number of genotypes to converge; though the values of s and t depend on the level of true ∞ . In this respect the measure NP(1) is closely behind NP(2).

The powers of the test for the non-parametric cases are given in Tables 14 and 15 while the figures for the parametric case are in Tables 16 and 17. Thennarasu[1] had already reported that the power of the test increases as the magnitude of σ_{se} decreases; therefore, this aspect was kept outside the purview of the present investigation. As expected the power of the test, in general, were higher in the parametric situations than in the non-parametric situations. It is also seen that the power increases rapidly with the increase in the number of genotypes. On the other hand the change of power from any increase in the number of environments, is rather small. A notable feature emerging from the data is that when the number of genotypes in the trial is fairly large the power efficiency of the non-parametric measures will be quite close to that of the parametric measures. So in these situations

Table 16. Comparison of power of the test (in a one way ANOVA) for different combinations of number of genotypes (t) and number of environments (s) at $\infty = 0.01$ for parametric measures

μ (Mea	n) = 1984 σ_{e}^{-}	$= 152.22 \sigma_G^2 =$	97.08 $\sigma_E^2 = 1$	121 $\sigma_{G \times E}^2 =$	324.44		
t	S	P(1)	P(2)	P(3)	P(4)	P(5)	
8	5	0.613	0.672	0.715	0.801	0.674	
12	5	0.803	0.845	Ò.935	0.918	0.879	
16	5	0.854	0.892	0.971	0.874	0.983	
20	5	0.915	0.984	0.998	1.000	0.997	
24	5	0.975	1.000	1.000	1.000	1.000	
8	10	0.618	0.701	0.723	0.839	0.719	
12	10	0.784	0.884	0.913	0.935	0.870	
16	10	0.901	0.994	0.958	1.000	0.974	
20	10	0.964	1.000	1.000	1.000	0.992	
24	10	0.998	1.000	1.000	1.000	1.000	
8	15	0.641	0.629	0.813	0.784	0.638	
12	15	0.709	0.874	0.892	0.984	0.711	
16	15	0.818	0.978	0.984	0.992	0.894	
20	15	0.935	0.991	0.992	0.999	0.955	
24	15	0.992	1.000	0.998	1.000	1.000	

	μ	(Mean) =	1984 ($\sigma_a^2 =$	152.22	$\sigma_c^2 =$	97.08	$\sigma_r^2 =$	1121	$\sigma^2_{C \times F}$	=	324.44
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Table 17.	Comparison of power of the test (in a one way ANOVA) for different
	combinations of number of genotypes (t) and number of environments
	(s) at $\propto = 0.05$ for parametric measures

е	G	E	$G \times E$			
S	P(1)	P(2)	P(3)	P(4)	P(5)	
5	0.703	0.743	0.804	0.839	0.749	
5	0.818	0.891	0.960	0.954	0.903	
5	0.903	0.918	0.982	0.986	0.994	
5	0.951	0.998	0.999	1.000	1.000	
5	0.982	1.000	1.000	1.000	1000	
10	0.709	0.739	0.834	0.872	0.813	
10	0.818	0.982	0.934	0.992	0.917	
10	0.953	1.000	0.965	1.000	0.991	
10	0.992	1.000	1.000	1.000	0.998	
10	1.000	1.000	1.000	1.000	1.000	
15	0.754	0.715	0.891	0.835	0.705	
15	0.845	0.913	0.902	0.989	0.819	
15	0.919	0.991	0.994	0.997	0.911	
15	0.972	0.997	0.998	1.000	0.992	
15	0.997	1.000	1.000	1.000	1.000	
	s 5 5 5 5 5 5 5 10 10 10 10 10 10 10 10 10 10 15 15 15 15 15	s P(1) 5 0.703 5 0.818 5 0.903 5 0.951 5 0.982 10 0.709 10 0.818 10 0.953 10 0.992 10 1.000 15 0.845 15 0.919 15 0.972 15 0.997	r r r r s $P(1)$ $P(2)$ 5 0.703 0.743 5 0.818 0.891 5 0.903 0.918 5 0.951 0.998 5 0.951 0.998 5 0.982 1.000 10 0.709 0.739 10 0.818 0.982 10 0.953 1.000 10 0.992 1.000 10 1.000 1.000 15 0.754 0.715 15 0.919 0.991 15 0.997 0.997 15 0.997 1.000	sP(1)P(2)P(3)50.7030.7430.80450.8180.8910.96050.9030.9180.98250.9510.9980.99950.9821.0001.000100.7090.7390.834100.8180.9820.934100.9921.0001.000101.0001.0001.000150.7540.7150.891150.9130.90215150.9720.9970.998150.9971.0001.000	sP(1)P(2)P(3)P(4)5 0.703 0.743 0.804 0.839 5 0.818 0.891 0.960 0.954 5 0.903 0.918 0.982 0.986 5 0.951 0.998 0.999 1.000 5 0.982 1.000 1.000 1.000 10 0.709 0.739 0.834 0.872 10 0.818 0.982 0.934 0.992 10 0.953 1.000 1.000 1.000 10 0.992 1.000 1.000 1.000 10 1.000 1.000 1.000 1.000 15 0.754 0.715 0.891 0.835 15 0.845 0.913 0.902 0.989 15 0.919 0.997 0.998 1.000 15 0.972 0.997 0.998 1.000 15 0.997 1.000 1.000 1.000	r r r r r sP(1)P(2)P(3)P(4)P(5)50.7030.7430.8040.8390.74950.8180.8910.9600.9540.90350.9030.9180.9820.9860.99450.9510.9980.9991.0001.00050.9821.0001.0001.0001000100.7090.7390.8340.8720.813100.8180.9820.9340.9920.917100.9531.0001.0001.0000.998101.0001.0001.0001.0001.000150.7540.7150.8910.8350.705150.8450.9130.9020.9890.819150.9720.9970.9981.0000.992150.9971.0001.0001.0000.992

 μ (Mean) = 1984 σ_1^2 = 152.22 σ_2^2 = 97.08 σ_2^2 = 1121 σ_2^2 = 324.44

the risk of selecting inferior genotypes from the use of non-parametric measures is minimal. Among the non-parametric measures, power of NP(2) is comparable to those of NP(3) and NP(4) and is definitely superior to both NP(1) and NP(5). We have already seen that the adequacy of normal approximation (in terms of \propto convergence) in the case both NP(1) and NP(2). Now we have noted that in respect of power efficiency NP(2) is superior to NP(1). Accordingly, in situations involving a large number of genotypes, which are to be performance-tested in a set of environments, whose number is neither too small nor too large the measure NP(2) can be used for selecting stable genotypes.

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INHERITANCE OF STEM RUST RESISTANCE IN A WHEAT-RYE RECOMBINANT LINE 'SELECTION 212'

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ABSTRACT

Selection 212, a wheat-rye recombinant developed through homoeologous recombination between wheat and rye chromosomes using monosomic 5B of variety Chinese Spring was studied for inheritance of resistance against stem rust pathogen (*Puccinia graminis* f. sp. *tritici*). The F₁, the F₂, the F₃, the BC₁F₁ and the BC₁F₂ generations of the crosses involving 'Selection 212' and two susceptible lines Agra Local and Chinese Spring were tested in seedlings with pathotypes 122 and 40A of *P. graminis tritici*. A single recessive gene that controlled resistance to both the pathotypes was determined. Correlated behaviour of the F₂ backcross families of the cross (Sel.212 × AL) × AL with both the pathotypes revealed that the same resistance gene is providing resistance to pathotypes 122 and 40A. In addition, an adult plant resistance gene *Sr2* was also identified.

Key Words : Wheat, rye (Secale cereale), stem rust (Puccinia graminis), inheritance, recessive

Stem rust of wheat caused by *Puccinia graminis* Pres. f.sp. *tritici* Eriks. and Henn. is the most devastating disease of wheat crop in warmer climates. Breeding for rust resistance is the most feasible and practical approach to check losses caused by rust diseases. The evolution of new pathotypes on widely grown resistant cultivars necessitates identification of new sources of resistance for continuous process of resistance breeding. In an effort 'Selection 212', (Sel. 212) a line with new source of resistance was developed by homoeologous chromosome recombination between wheat and rye using monosomic 5B of variety Chinese Spring [1]. Sel. 212 when tested at seedling stage with 20 pathotypes of *P. graminis tritici* was found resistant to all the pathotypes [2]. The present study reports the inheritance of resistance to stem rust at seedling and adult plant growth stages using pathotypes 122 and 40A which identify resistance in Sel. 212, transferred from rye.